Online game players’ action sequences, while important to understand their behavior, usually contain noise and/or redundancy, making them unnecessarily long. To acquire briefer sequences representative of players’ features, we apply the Haar wavelet transform to action sequences and reconstruct them from selected wavelet coefficients. Results indicate that this approach is effective in classification when the $k$-nearest neighbor classifier is used to classify players based on dynamic time warping distances between reconstructed sequences.

**Keywords:** online game, player classification, wavelet transform, dynamic time warping, action sequences

1. Introduction

Keeping online game players playing requires finding and fulfilling players’ demands and tailoring appropriately contents to each player or group of players. In virtual worlds such as online games, players are typically identified by performance type such as killer, achiever, explorer, and socializer [1]. Such types should be exploited to provide game contents that players favor. Examples of content include more hunting opportunities for killers, a wider variety of collectable items for achievers, longer missions for explorers, and a higher frequency of social events for socializers.

Online game players’ action sequences are crucial for classifying player types, but noise or redundancy makes them needlessly long. Rather than directly using action sequences in classifying players, we previously used normalized action frequency vectors (NAFV) [2] and hidden markov models (HMM) [3]. The NAFV requires no parameter settings, costs relatively little, and effectively classifies players whose action frequency distinctly differs. It is less effective, however, when differences are less apparent despite dissimilar action sequences. The HMM [4] classifies sequence data well, but its performance depends on the initial structure and parameters.

We proposed a parameter-free approach [5] using action transition probability and considering action information in frequency and order. However, we found this approach unsuitable for classifying players with similar local behaviors but with different global structures, such as classification of Type-I players performing mission A before mission B and Type-II players vice versa. This is because the action transition probability represents only local changes in the sequence of interest.

In this paper, we apply Haar wavelet transform [6] to action sequences and reconstruct them from selected wavelet coefficients. By this, more compact sequences are obtained representing important player features covering both local and global information. We employ the $k$-nearest neighbor classifier [7] to classify unknown players and dynamic time warping [8] to calculate distances between the reconstructed sequence of an unknown player and those of known players. We evaluate this approach with action sequences from an online game, “The ICE” we are developing.

Related work in the literature focuses on players’ trails or time series of locations visited, such as using trails to determine the distance over time among members of a social group [9] or a visualization tool for visualizing player flows in virtual environments such as virtual museums [10]. Other work focuses on visualizing important parts of trails [11] and on player clustering based on trails [12].

This paper is organized as follows: Section 2 discusses the Haar wavelet transform, Section 3 details dynamic time warping, Sections 4 and 5 propose selecting wavelet coefficients and evaluate performance, and Section 6 summarizes the paper and mentions future work.

2. Haar Wavelet Transform

In the Haar wavelet transform concept, decomposition involves obtaining Haar wavelet coefficients from an action sequence. Reconstruction involves recovering the original sequence from obtained coefficients. Our proposal for selecting coefficients to achieve more compact sequences representing important features is detailed in Section 4.

We assume that length $L$ of a sequence is a power of 2 and $q = \log_2(L)$. The $i$th Haar wavelet coefficient at...
resolution order \( k \), \( d_{(k,0)} \) is derived by

\[
d_{(k,0)} = \frac{x_{(k+1,2i-1)} - x_{(k+1,2i)}}{2}
\] .... (1)

where \( x_{(k,0)} = \frac{x_{(k+1,2i-1)} + x_{(k+1,2i)}}{2} \) is the \( i \)th value at order \( k \) between two corresponding adjacent values in order \( k+1 \). Note that with this representation, \( k_{\text{max}} = q \), and the original sequence is represented by \( x = x_{(q,1)}, x_{(q,2)}, \ldots, x_{(q,L)} \). An example of Haar wavelet decomposition of the sequence 9, 7, 1, 2, 4, 8, 5, 2 is shown in Table 1.

Reconstruction of a given sequence from its Haar wavelet coefficients and averages is done using the following formulas:

\[
x_{(k,2i-1)} = x_{(k-1,i)} + d_{(k-1,i)}
\] .... (2)

\[
x_{(k,2i)} = x_{(k-1,i)} - d_{(k-1,i)}
\] .... (3)

### 3. Dynamic Time Warping for Action Sequences

#### 3.1. Action Coding

Let \( O \) denote the set of action symbols of interest and \( |O| \) their number. As in [8], action sequence \( S = S(1), S(2), \ldots, S(L) \) is numerically coded into \( |O| \times L \) time-series matrix \( X = [X(1), X(2), \ldots, X(L)] \), where \( X(i) \) is a column vector with the element indexing the action symbol of \( S(i) \) being 1 and others 0.

Consider, for example, the set of action symbols \( O = \{A, B, C\} \), and thus \( |O| = 3 \), where symbols \( A, B, \) and \( C \) are represented by column vectors \([100]^T\), \([010]^T\), and \([001]^T\). In an action sequence such as \( S = A, B, C, C \), it is coded to \( X = [[100]^T, [010]^T, [001]^T, [001]^T] \).

#### 3.2. Dynamic Time Warping

Two time series of interest are considered similar if they have the same structures, i.e., rise and fall patterns, although they might have different scales on the time axis. A good measurement for deriving the distance between such series is the dynamic time warping (DTW) distance. The DTW distance between time-series matrices \( X \) and \( Y \), \( D(X,Y) \), having lengths \( L_X \) and \( L_Y \), is defined as follows [8]:

\[
D(X,Y) = g(L_X, L_Y)
\] .... (4)

where

\[
g(i,j) = \min \begin{cases} g(i, j-1) + d(i,j) \\ g(i-1, j-1) + d(i,j) \\ g(i-1, j) + d(i,j) \end{cases}
\] .... (5)

\[
g(i,0) = \begin{cases} 0 & i = 0 \\ \infty & i > 0 \end{cases}
\] .... (6)

\[
g(0,j) = \begin{cases} 0 & j = 0 \\ \infty & j > 0 \end{cases}
\] .... (7)

and \( d(i,j) \) is the Euclidean distance between \( X(i) \) and \( Y(j) \).

Consider, for example, the set of symbols \( O = \{A, B, C, D, E, F\} \) and two action sequences \( x = C, D, F, E, B \) and \( y = C, A, D, D, F, E, B \). The DTW distance between corresponding time-series matrices \( X \) and \( Y \) (Fig. 1), \( D(X,Y) \), is 1.4, derived as shown in Fig. 2.

### 4. Reduction of Action Sequences

Given the set of action symbols \( O \), below, we describe our procedure for reducing the length of an action sequence of interest. As an example, we use action sequence \( x = A, B, C, C, A, B, C, C, A, A, B, B, B, A, A \) where \( O = \{A, B, C\} \) and thus \( |O| = 3 \).

- Derive corresponding time-series matrix \( X \) for action
sequence of interest \( x \) having length \( L_1 \). In our example, time-series matrix \( X \) is shown in Fig. 3.

- Decompose each row in \( X \) to obtain Haar wavelet coefficients. Resulting coefficients for \( X \) are given in Fig. 4.

- Reconstruct each row in \( X \) with selected Haar wavelet coefficients as follows:
  Following the same recipe in [6], the number of Haar wavelet coefficients used to evaluate performance is heuristically set to \( \min(L-1, \lfloor \log_2 L \times 4 \rfloor) \). Reconstruction of each row in \( X \) is started from the coefficient at the lowest resolution order, i.e., \( d(1,1) \), to those at the next higher order, etc. At a given resolution order, when the number of remaining coefficients that must be selected for reconstruction is less than the number of coefficients in that order, we propose selecting remaining coefficients based on their total energy value in decreasing order, where total energy

  of \( d_{(k,i)} \), \( E_{(k,i)} \), is defined as

  \[
  E_{(k,i)} = \sum_{n=1}^{[\theta]} d_{(n,k,i)}^2 \quad \ldots \quad \ldots \quad \ldots \quad \ldots \quad (8)
  \]

  where \( d_{(n,k,i)} \) is \( d_{(k,i)} \) decomposed at row \( n \) of \( X \). Remaining coefficients are then reset to zero. Assume that four coefficients are selected in our example; \( X \) resulting after selection of coefficients is shown in Fig. 5.

- Reconstruct the action sequence with the above coefficients (Fig. 6).

- Reduce the size of \( X \) by sampling down a group of repetitive and consecutive elements at each reconstructed row to one element [6]. The reduced \( X \) is given in Fig. 7.

---

1. We assume that length \( L \) of each action sequence is adjusted so that \( L \) is a power of 2.
5. Performance Evaluation

5.1. Players’ Logs

We obtained players’ logs from the online game The ICE, now being developed at our laboratory, a screen shot of which is shown in Fig. 8. The main game objects involved in the study were the mission master (MM), who assigned a mission to a player character (PC); three non-player characters (NPCs), Ceris, Rodth, and Gelec, statically located at different locations and with whom PC must interact (chat, help, trade)- to complete the assigned mission; the item-shop NPC from which PC bought items; and monster ants, randomly located throughout the map, that PC must exterminate. Actions available in The ICE are summarized in Table 2, where for Talk the initial letter of a corresponding NPC is used.

A group of 30 male test-players, on average 20 years of age, participated. These players consisted of third-year and fourth-year computer science undergraduate students with no experience in playing The ICE. They could move freely and attempt any command, but were not allowed to do any unassigned mission. A brief description of each mission is given as follows:

**M1**: Item Delivery. PC must deliver an item from MM to a specific NPC and then deliver an item from that NPC to another NPC, etc.

**M2**: Item Trade. PC must trade with NPCs to increase the amount of money initially provided by MM. PC uses the initial money to buy one of the three items from the item-shop NPC and sells the item at a higher price to one of the three NPCs, who only buy a particular item.

**M3**: Monster Ant Extermination. PC must help Rodth by exterminating five monster ants.

After checking players’ logs, we found, not surprisingly, that most players soon dropped their game missions to play the game on their own. This made it difficult to correctly classify them based on their logs. To classify players, below, we selected four players from each subgroup who played the assigned missions. Table 3 shows the mean and variance of lengths before and after action sequence are shorten.

5.2. Player Classification

As a classifier, we use the $k$ nearest neighbor ($k$-nn) classifier. We determined classification performance in three cases, mutually differing in the calculation of the distance between a pair of players, i.e.,

**Case 1**: The sum of DTW distances between rows of the reduced time-series matrices was used.

**Case 2**: The sum of DTW distances between rows of original time-series matrices was used.

---

**Table 2.** Action list of The ICE.

<table>
<thead>
<tr>
<th>Action</th>
<th>Symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>Attack with a snow ball</td>
<td>a</td>
</tr>
<tr>
<td>Chat</td>
<td>c</td>
</tr>
<tr>
<td>Walk</td>
<td>w</td>
</tr>
<tr>
<td>Trade</td>
<td>t</td>
</tr>
<tr>
<td>Talk (*)</td>
<td>*</td>
</tr>
<tr>
<td>Pick up potion</td>
<td>p</td>
</tr>
<tr>
<td>Use potion</td>
<td>u</td>
</tr>
<tr>
<td>Dead</td>
<td>d</td>
</tr>
<tr>
<td>Warp</td>
<td>r</td>
</tr>
</tbody>
</table>

**Table 3.** Action-sequence length statistics before and after reduction.

<table>
<thead>
<tr>
<th></th>
<th>MEAN</th>
<th>VAR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Before</td>
<td>885.8</td>
<td>286504.7</td>
</tr>
<tr>
<td>After</td>
<td>30.1</td>
<td>13.9</td>
</tr>
</tbody>
</table>

They could move freely and attempt any command, but were not allowed to do any unassigned mission. A brief description of each mission is given as follows:

**M1**: Item Delivery. PC must deliver an item from MM to a specific NPC and then deliver an item from that NPC to another NPC, etc.

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Case 3: The sum of Euclidean distances between rows of action-transition-probability matrices [5] was used.

Tables 4-6 show the classification performance for each case over three variations of k, in which individual results were obtained by leave-one-out cross-validation [7]. The i,jth element indicates the number of times the k-nn classifier labels an unknown player of subgroup Gi to subgroup Gj. The k-nn classifier performance in case 1 outperforms those of other cases. Analyzing results, we found that the k-nn in case 2 had difficulty in identifying G3 because partial sequences of multiple attacks typically seen in M3 were also seen in M2. The k-nn in case 1 presented no such difficulty indicating that the proposed distance measure is more reliable. The k-nn in case 3 had the worst performance because the distance measure in [5] could not cope with global structures, i.e., mission sequences. However, it could well classify the players in G1 because they walked a lot during play, making their transition probability from walk to classify the players in G1 because they walked a lot during playing, indicating that the proposed distance measure is more reliable.

6. Conclusions and Future Work

We have described how to calculate the distance between players’ action sequences for classifying online-game players. The described distance measure is the dynamic time warping distance between the reduced time-series matrices of a pair of players of interest. We applied the Haar wavelet transform to decompose time-series matrices derived from action sequences and to reconstruct them based on a set of Haar wavelet coefficients selected by our energy-based proposal. We evaluated performance using the online game The ICE, indicating that the k-nn classifier using the aforementioned distance measure outperforms those using conventional distance measures. We plan to apply the distance measure to online-game player clustering and visualization.

References:


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